First operation of a Harmonic Lasing Self-Seeded FEL
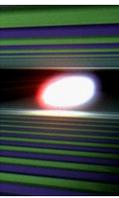
E. Schneidmiller and M. Yurkov

- Harmonic lasing

- Harmonic lasing self-seeded (HLSS) FEL

- Experiments at FLASH

• In a planar undulator (K ~ 1 or K >1) the odd harmonics can be radiated on-axis (widely used in SR sources)

• For coherent emission a mechanism is required to create coherent microbunching at harmonic frequencies

• There are two basic mechanisms in FELs:
-   Nonlinear harmonic generation
-   Harmonic lasing

We consider SASE process in a baseline XFEL undulator

Nonlinear harmonic generation
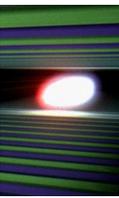
- When lasing at the fundamental frequency approaches saturation, the density modulation becomes nonlinear (contains higher harmonics)
- Odd harmonics are radiated then on-axis
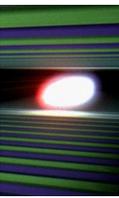- Well-known process, studied in many papers

Microbunching at saturation
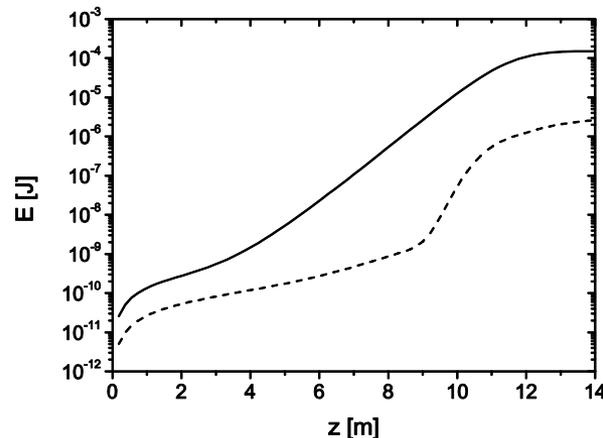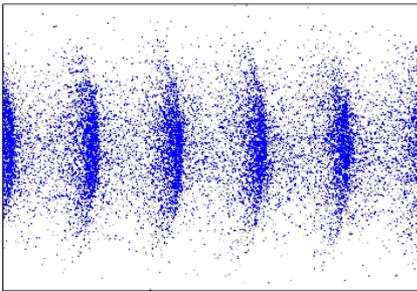

1st: solid
3rd: dash

3rd harmonic is driven by the fundamental

Occurs whenever an FEL reaches saturation; studied and used at FLASH, LCLS etc.

- Power of 3rd harmonic is about 1% of saturation power of the fundamental (and much smaller for higher harmonics)

- Relative bandwidth is approximately the same (contrary to 1/h in the case of spontaneous emission)

- Shot-to-shot intensity fluctuations are much stronger

- Transverse coherence is worse

In short, nonlinear harmonics are much less brilliant and less stable than the fundamental
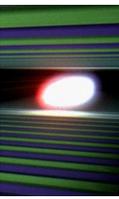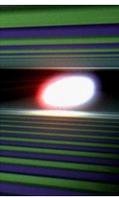
- Harmonic lasing is an FEL instability developing independently of the fundamental (in linear regime)
- We have to disrupt the fundamental to let a harmonic saturate
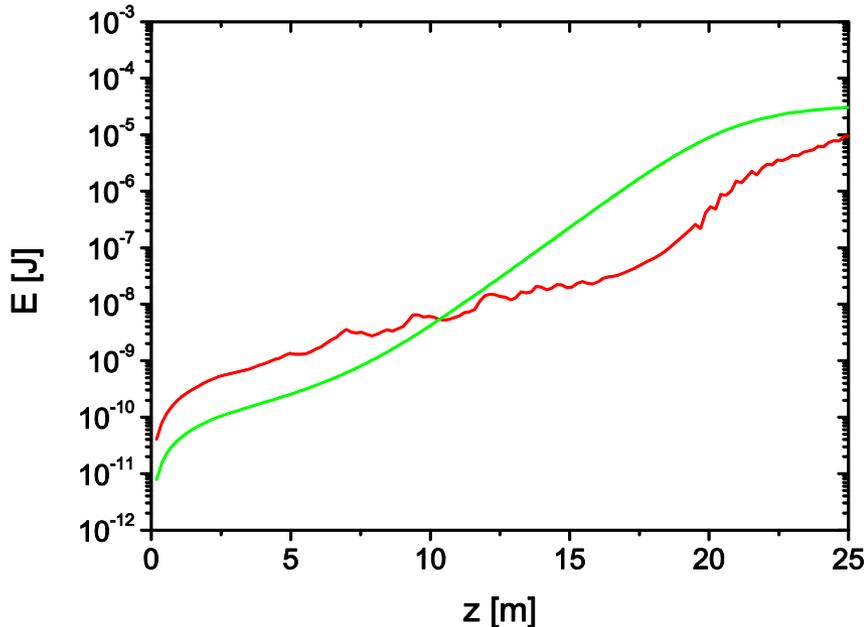
1st: red
3rd: green

the fundamental is disrupted by phase shifters

- Saturation efficiency of h-th harmonic scales as $\sim \lambda_w/(hL_{sat})$

- Relative rms bandwidth scales as $\sim \lambda_w/(hL_{sat})$

- Shot-to-shot intensity fluctuations are comparable (the same statistics)

- Good transverse coherence

Brilliance is comparable to that of the fundamental!
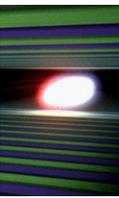
• First theoretical consideration for low-gain FELs more than 30 years ago (Colson, 1981)

• Several successful experiments with FEL oscillators in infrared range (1988-2010)
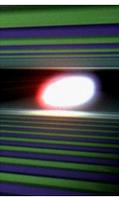
• High-gain FELs:

1D theory of harmonic lasing:

    Murphy, Pellegrini, Bonifacio, 1985
    Bonifacio, De Salvo, Pierini, 1990
   McNeil et al., 2005

3D theory (everything included):

    Z. Huang and K.-J. Kim, 2000

• Eigenvalue equation for calculation of gain length of harmonic lasing including all important effects: emittance, betatron motion, diffraction of radiation, energy spread etc.
• Numerical example for LCLS: NO harmonic lasing.
Reason: too large emittance and energy spread anticipated at that time.

$$\bar{\Phi}_{nm}(p) = -\frac{h^2 A_{JJh}^2}{A_{JJ1}^2(2\,\mathrm{i}\,hB\hat{\Lambda} - p^2)} \int\limits_0^\infty \mathrm{d}\,p'p'\bar{\Phi}_{nm}(p')$$

$$\times \int\limits_0^\infty \mathrm{d}\,\zeta \frac{\zeta}{(1 - \mathrm{i}\,hB\hat{k}_\beta^2\zeta/2)^2} \exp\left[-\frac{h^2\hat{\Lambda}_\mathrm{T}^2\zeta^2}{2} - (\hat{\Lambda} + \mathrm{i}\,\hat{C})\zeta\right]$$

$$\times \exp\left[-\frac{p^2 + p'^2}{4(1 - \mathrm{i}\,hB\hat{k}_\beta^2\zeta/2)}\right] I_n\left[\frac{pp'\cos(\hat{k}_\beta\zeta)}{2(1 - \mathrm{i}\,hB\hat{k}_\beta^2\zeta/2)}\right].$$

Our revision in 2012
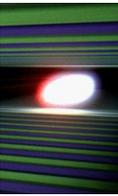
- Found simple parametrization of the gain length and upgraded FEL code FAST
- Could then analyze parameter space (with optimistic conclusions)
- Proposed new methods for suppression of the fundamental
- Discovered qualitatively new effect of anomalously strong harmonic lasing for thin electron beams
- Suggested method for improvement of spectral brightness (later called HLSS FEL)
- Considered practical applications in different facilities

Our conclusion: the option must be seriously considered!
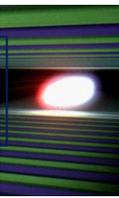
A. Harmonic lasing (with the suppressed fundamental) at some WL vs fundamental lasing at the same WL with reduced K.

$$\frac{L_g^{(1K)}}{L_g^{(h)}} = \frac{h^{1/2}KA_{JJh}(K)}{K_{re}A_{JJ1}(K_{re})}$$
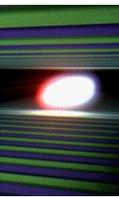
$$K_{re}^2 = \frac{1+K^2}{h} - 1$$

B. Harmonic lasing (with the suppressed fundamental) at some WL vs fundamental lasing at the same WL with increased beam energy.

$$\frac{L_g^{(1\gamma)}}{L_g^{(h)}} = \frac{h^{5/6}A_{JJh}(K)}{A_{JJ1}(K)}$$
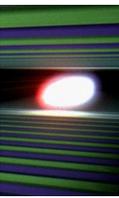
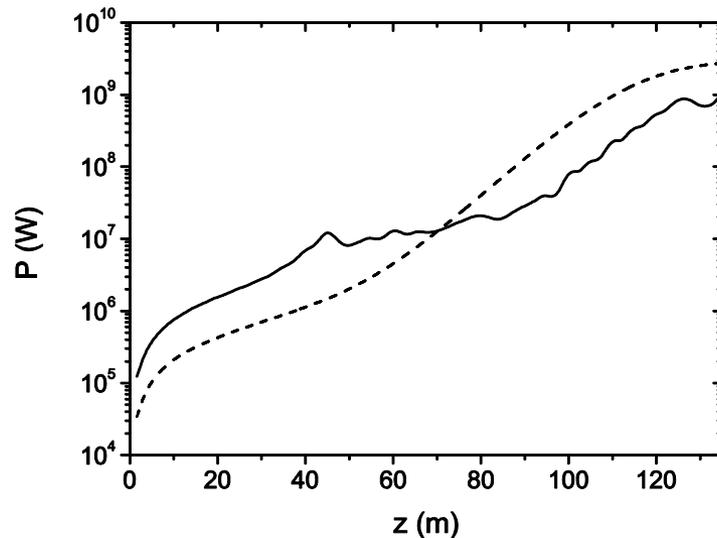Negligible energy spread, beta is optimized in all cases
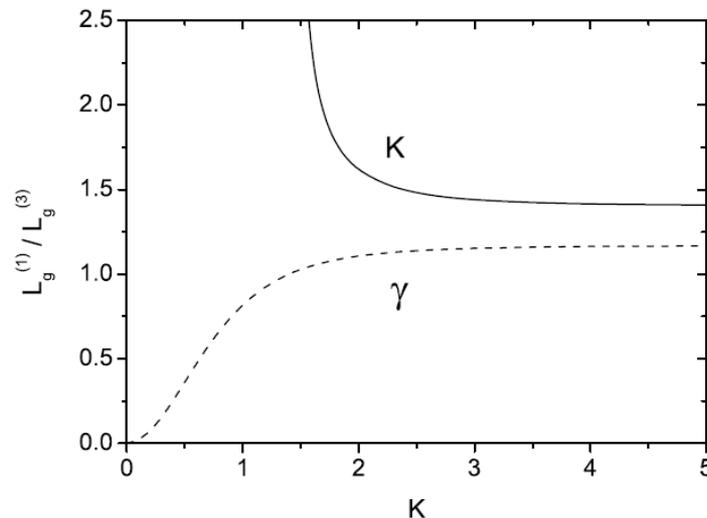
Better than in 1D!

- Phase shifters

- Spectral filtering

- Switching between 3rd and 5th harmonics

3rd harmonic lasing at 62 keV (0.2 A). Beam parameters for 100 pC from s2e (quantum diffusion in the undulator added), energy 17.5 GeV. With 20 pC bunch one can even reach 100 keV.
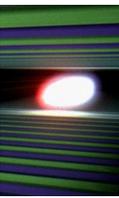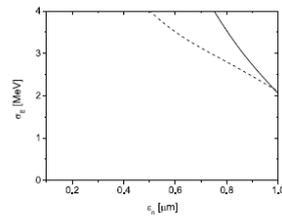

1st: solid
3rd: dash

bandwidth is 2×10^{-4} (FWHM)

There are plans for MID instrument (A. Madsen);
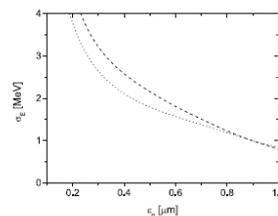users are interested; MAC recommended.

CW upgrade of the European XFEL

It is expected to have 7 GeV in CW mode and 10 GeV in long pulse mode with 35% duty factor.

10 GeV **7 GeV**

1 A

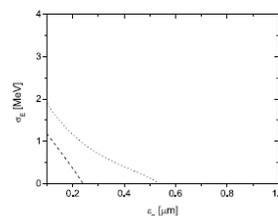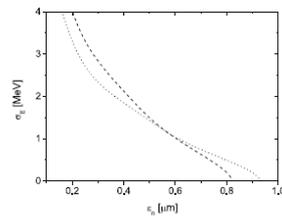**0.75 A**
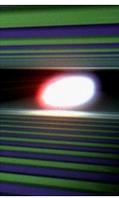
0.5 A

1st: solid
3rd: dash
5th: dot
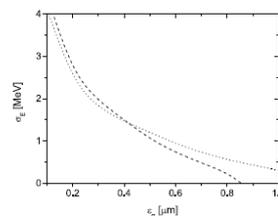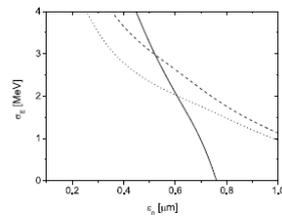
Brinkmann, Schneidmiller, Sekutowicz, Yurkov, NIMA 768(2014)20

Possible upgrade of FLASH

Lasing down to 1.3 nm is desirable. Making use of 3rd harmonic lasing we can reach this WL with present accelerator energy of 1.25 GeV.

Electron beam	Value
Energy	1.25 GeV
Charge	150 pC
Peak current	2.5 kA
Rms normalized slice emittance	0.5 μm
Rms slice energy spread	250 keV
Rms pulse duration	24 fs

Undulator	Value
Period	2.3 cm
Minimum gap	9 mm
K_{rms} (at minimum gap)	1
Beta-function	7 m
Net magnetic length	25 m
Total length	34.5 m

1st: solid
3rd: dash
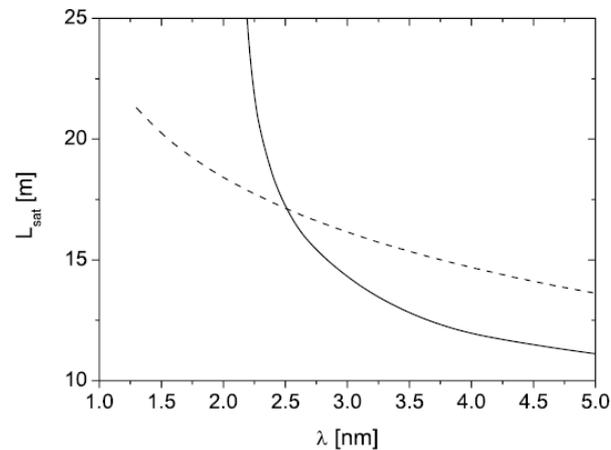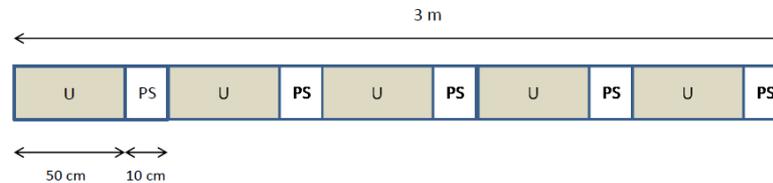
Schneidmiller, Yurkov, NIMA 717(2013)20

Wavelength	1.3 nm
Averaged peak power	1 GW
Pulse energy	30 μJ
Shot-to-shot fluctuations	< 10 %
Pulse duration (FWHM)	30 fs
Bandwidth (FWHM)	0.1 %
Angular divergence (FWHM)	10 μrad
Peak brilliance	10^{31} ph./(s mrad^2 mm^2 0.1% BW)

1st: solid
3rd: dash

HLSS FEL (Harmonic Lasing Self-Seeded FEL)
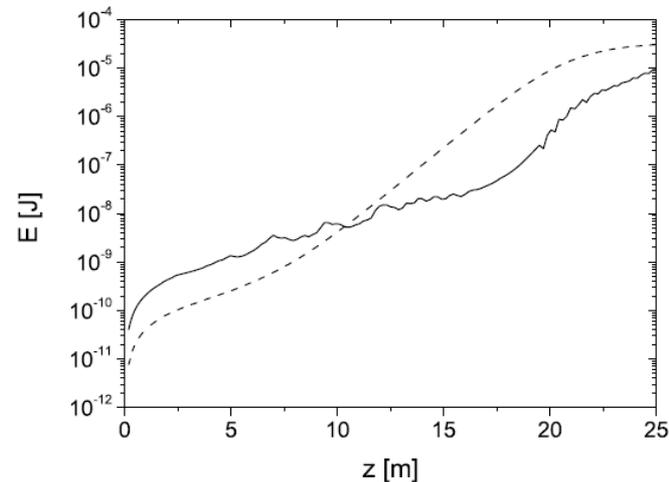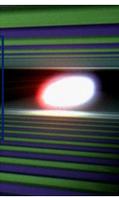
We proposed a simple trick for improvement of spectral brightness in a gap-tunable undulator: harmonic lasing in linear regime (with narrow bandwidth) in the first part of the undulator, then reducing K and reaching saturation at the fundamental. Then we have high power and narrow BW.

E. Schneidmiller and M. Yurkov, Phys. Rev. ST-AB 15(2012)080702

exponential gain   saturation

$\lambda_{\mathrm{res}} = h\lambda_1$ $\lambda_{res} = \lambda_1$

larger K   smaller K
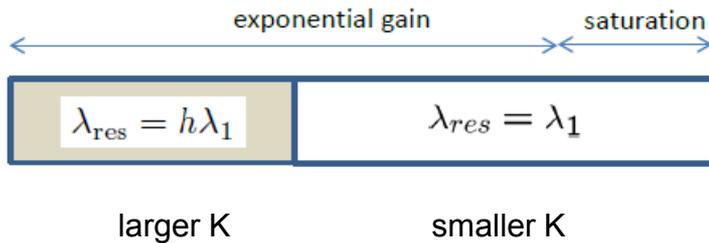
Bandwidth reduction factor:

$$R \simeq h \, \frac{\sqrt{L_{\mathrm{w}}^{(1)} L_{\mathrm{sat},h}}}{L_{\mathrm{sat},1}}$$

Typically R = 0.6-0.9 h

The fundamental and all harmonics have to stay well below saturation in the first part of the undulator. Use of phase shifters in the first undulator is optional.

1.5 nm   0.3 nm

HLSS   SASE
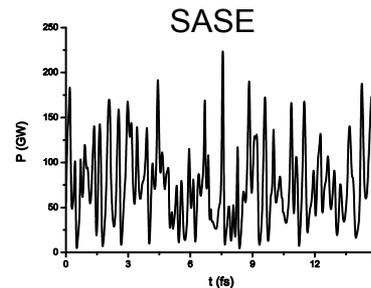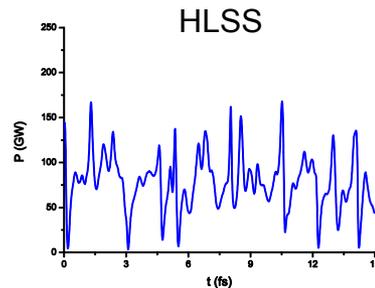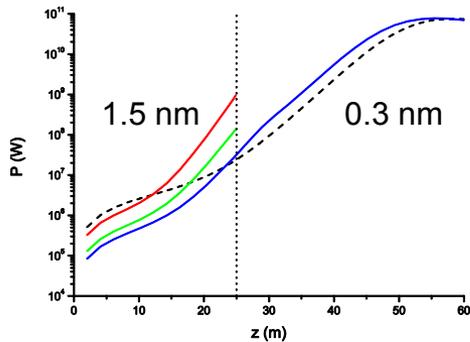
E. Schneidmiller and
M. Yurkov, FEL'13
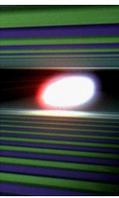
- Post-saturation taper works better for seeded FELs;

- Coherence length does not have to equal bunch length, even moderate increase is sufficient;

- In self-seeding schemes the saturation length is about twice that of SASE: less space for post-saturation taper;

- HLSS saturates even earlier than SASE: more space for post-saturation taper, more power can be extracted.

HLSS FEL seems to be the optimal solution for maximizing FEL power.

RF Stations

Accelerating Structures

sFLASH

Soft X-ray Undulators

Photon Diagnostics

FLASH1

THz

RF Gun Lasers

Bunch Compressors

FLASH2

5 MeV   150 MeV   450 MeV   1250 MeV

Beam Dump

FEL Experiments

315 m
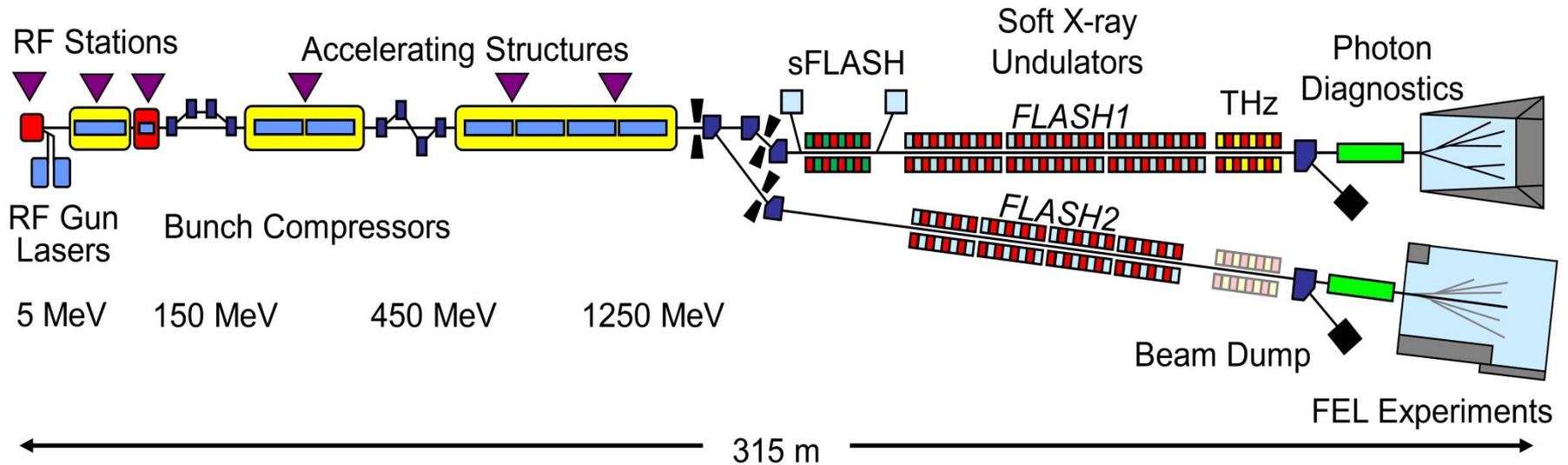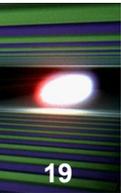
■ Undulators

	Period	Length	
■			
■ FLASH1:	2.73 cm	27 m (6 x 4.5 m modules)	fixed gap
■ FLASH2:	3.14 cm	30 m (12 x 2.5 m modules)	variable gap
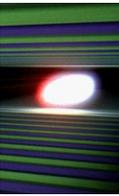
exponential gain   **saturation** (actually, no saturation)

| $\lambda_{\mathrm{res}} = h\lambda_1$	$\lambda_{\mathrm{res}} = \lambda_1$
3 undulators	7 undulators
21 nm	7 nm

K-scan of the undulators: only 1st (red);
1st and 2nd (green) ; 1st, 2nd and 3rd (blue)
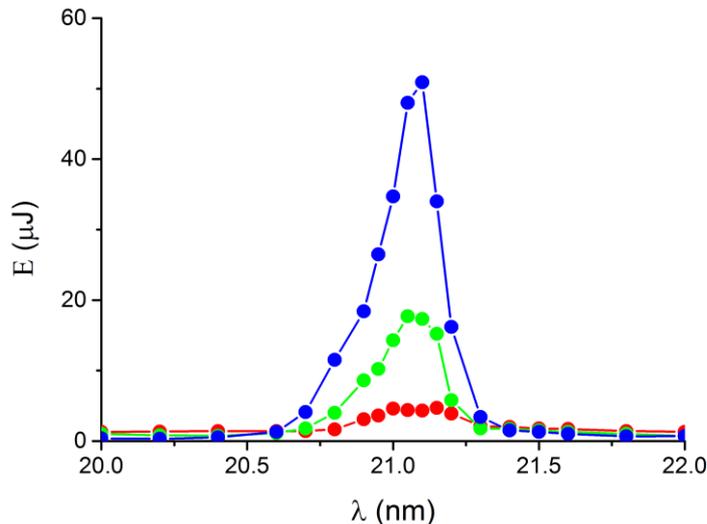
- Normal SASE at 7 nm in 10 undulators: 12 uJ (exponential gain)
- Detuning first (first two, first three) undulator sections: sharp intensity drop
- Coming close to 21 nm: sharp increase, resonant behavior
- With 3 undulators we have 51 uJ instead of 12 uJ; gain length of the 3rd harmonic is shorter than that of the fundamental at 7 nm!
- Nonlinear harmonic generation in the first part is absolutely excluded: pulse energy at 21 nm after 3 undulators was 40 nJ (but about 200 uJ at saturation): 4 orders of magnitude
- Results can only be explained by 3rd harmonic lasing at 7 nm

E. Schneidmiller et al., Phys. Rev. AB 20 (2017)020705
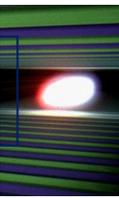
exponential gain   saturation   (actually, no saturation)

$\lambda_{res} = h\lambda_1$	$\lambda_{res} = \lambda_1$

4 undulators   6 undulators
33 nm   11 nm

- Lower electron energy
- Normal SASE at 11 nm with 10 undulators and HLSS with 4+6 undulators
- Nonlinear harmonic generation in the first part is excluded: three orders below saturation
- An attempt to see bandwidth reduction

K-scan of the first 4 undulators
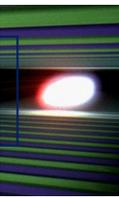
Spectral measurements
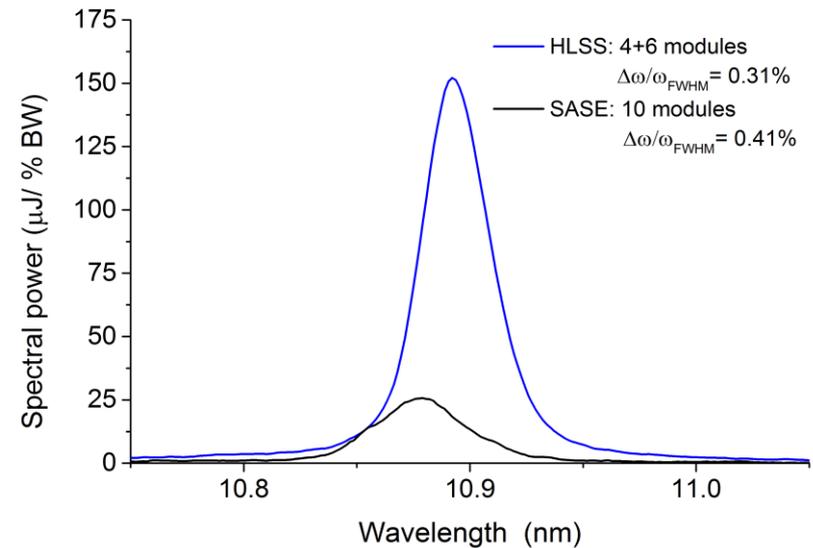
HLSS (4+6)

SASE (10)
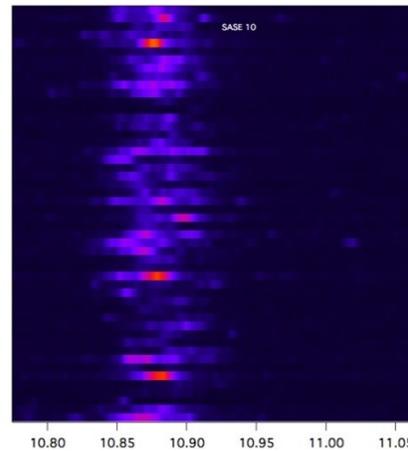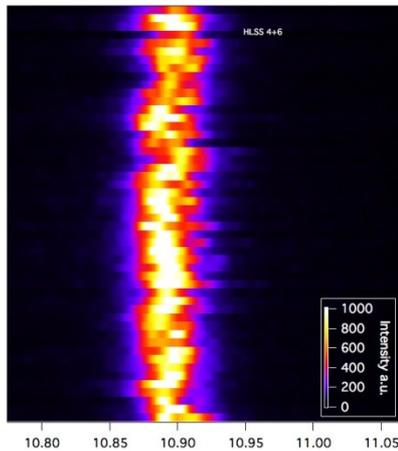
Expectations

$$R \simeq h \frac{\sqrt{L_{\text{w}}^{(1)} L_{\text{sat},h}}}{L_{\text{sat},1}}$$

R = 1.7

Measured: R = 1.3

Energy chirp!
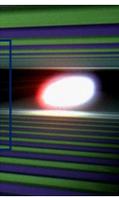
Statistical determination of an increase of the coherence time
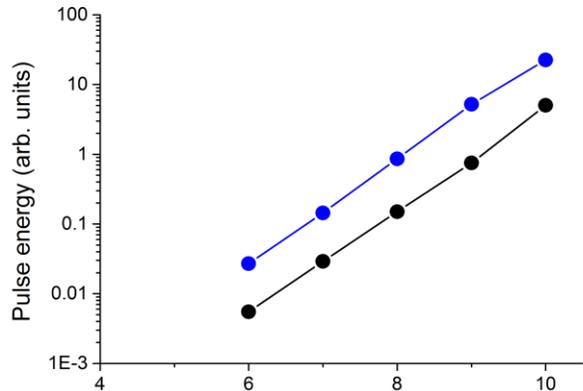
$$M_l \propto 1/L^{coh}$$

$$M_l = 1/\sigma^2$$

$$\frac{L^{coh}_{HLSS}}{L^{coh}_{SASE}} = \frac{\sigma^2_{HLSS}}{\sigma^2_{SASE}} \simeq 1.8$$

Expectations

$$R \simeq h \frac{\sqrt{L^{(1)}_w L_{sat,h}}}{L_{sat,1}}$$

R = 1.7

SASE (black) and HLSS (blue)
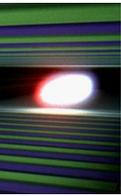
exponential gain   saturation

| $\lambda_{\rm res} = h\lambda_1$ | $\lambda_{\rm res} = \lambda_1$ |

4 undulators   8 undulators
45 nm   15 nm
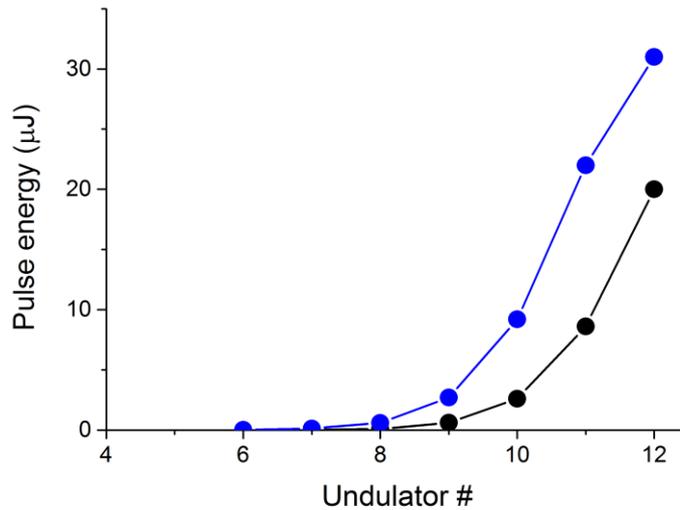
Post-saturation taper is applied:
SASE (black) and HLSS (blue)
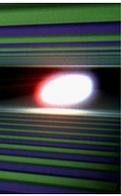
exponential gain   saturation

$\lambda_{\rm res} = h\lambda_1$	$\lambda_{\rm res} = \lambda_1$
3 undulators	9 undulators
13.5 nm	4.5 nm
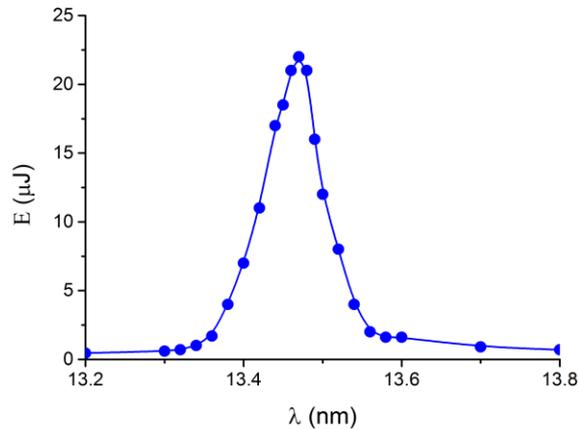
K-scan of the first 3 undulators
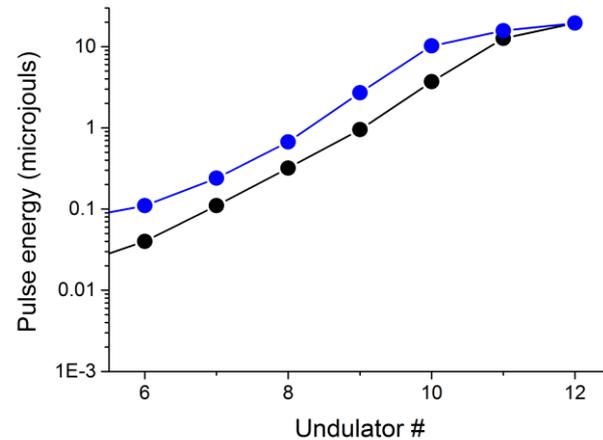
Gain curve:

SASE (black) and HLSS (blue)
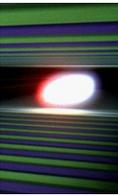
- HLSS FEL worked at PAL XFEL down to 1 nm (presented at FEL'17)

- Plans for fresh slice harmonic lasing at LCLS

- We plan experiments at the European XFEL

- Interest at Swiss XFEL and SACLA

Conclusions
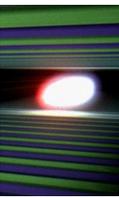
- Harmonic lasing is an interesting option for XFELs;

- Main application I: extension of photon energy range (60-100 keV for the European XFEL, also CW upgrade; FLASH up to 1 keV);

- Main application II: bandwidth reduction and brilliance increase (HLSS) + improved post-saturation taper;

- Successful demonstration of HLSS principle at FLASH2;

- First evidence of harmonic lasing in a high-gain FEL and at a short wavelength (4.5 nm) paves the way for its applications in X-ray FEL facilities.

- A growing interest at different facilities

Backup slides

exponential gain → saturation

$$\lambda_{\rm res} = h\lambda_1 \qquad \lambda_{\rm res} = \lambda_1$$
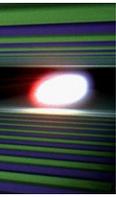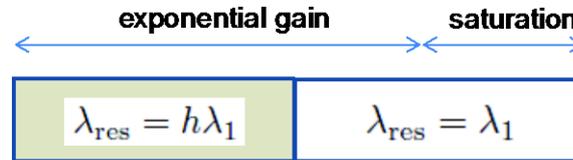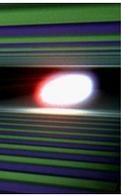
No tapering (log scale)
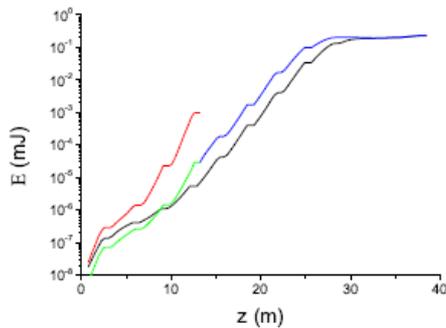
Figure 2: FEL pulse energy versus undulator length. In the first part of the undulator (tuned to the resonance with 39 nm) the first (red) and the third (green) harmonics are shown. The third harmonic continues to get amplified in the second part of the undulator (now as the fundamental) tuned to 13 nm (shown in blue). A reference case of lasing at 13 nm on the fundamental in the whole undulator with constant K-value is shown in black.

Tapering (linear scale)
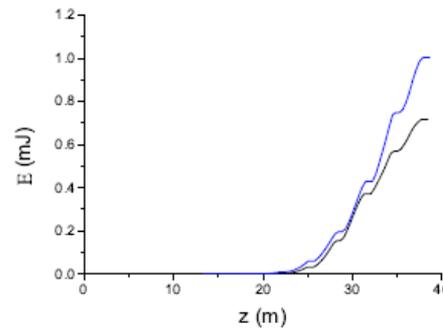
Figure 3: FEL pulse energy versus undulator length when the post-saturation taper is applied. HLSS case is shown in blue, and the SASE case - in black.

Spectral density

Figure 4: Spectral density of the radiation energy for HLSS FEL configuration (blue) and for SASE FEL (black).

$$R \simeq h \, \frac{\sqrt{L_{\rm w}^{(1)} L_{\rm sat,h}}}{L_{\rm sat,1}}$$

R = 0.6 h = 1.8

E. Schneidmiller and M. Yurkov, Proc. IPAC2016, MOPOW009

Generalization of formulas from   Saldin, Schneidmiller and Yurkov, Opt. Commun. 235(2004)415

$$L_g \simeq L_{g0} \left(1 + \delta\right)$$ field gain length

$$A_{JJh}(K) = J_{(h-1)/2}\left(\frac{hK^2}{2(1+K^2)}\right) - J_{(h+1)/2}\left(\frac{hK^2}{2(1+K^2)}\right)$$

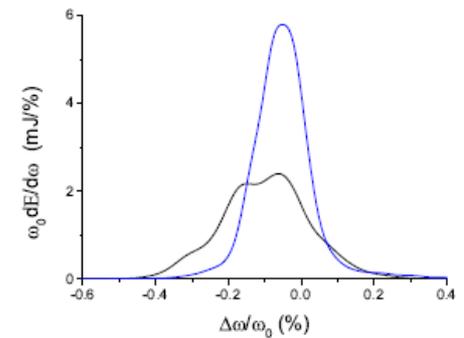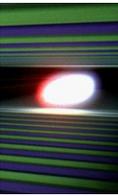$$L_{g0} = 1.67 \left(\frac{I_A}{I}\right)^{1/2} \frac{(\epsilon_n \lambda_{\mathrm{w}})^{5/6}}{\lambda_h^{2/3}} \frac{(1+K^2)^{1/3}}{h^{5/6} K A_{JJh}}$$

$$\delta = 131 \frac{I_A}{I} \frac{\epsilon_n^{5/4}}{\lambda_h^{1/8} \lambda_{\mathrm{w}}^{9/8}} \frac{h^{9/8} \sigma_\gamma^2}{(K A_{JJh})^2 (1+K^2)^{1/8}}$$

$$\beta_{\mathrm{opt}} \simeq 11.2 \left(\frac{I_A}{I}\right)^{1/2} \frac{\epsilon_n^{3/2} \lambda_{\mathrm{w}}^{1/2}}{\lambda_h h^{1/2} K A_{JJh}} \left(1 + 8\delta\right)^{-1/3}$$

$$L_g(\beta) \simeq L_g(\beta_{\mathrm{opt}}) \left[1 + \frac{(\beta - \beta_{\mathrm{opt}})^2 (1 + 8\delta)}{4\beta_{\mathrm{opt}}^2}\right]^{1/6}$$ for $\beta > \beta_{\mathrm{opt}}$ new also for the fundamental
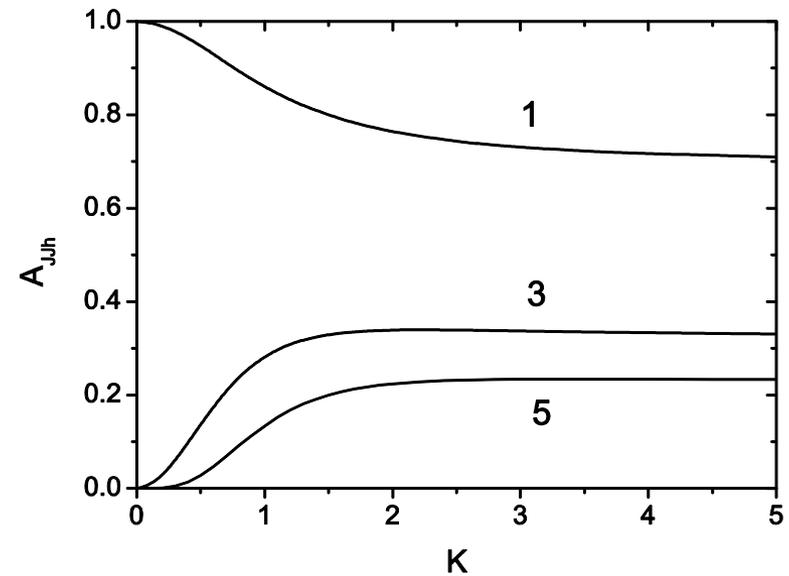
$$2\pi\epsilon/\lambda \sim 1 \qquad \text{or} \qquad 2\pi\epsilon/\lambda \gg 1$$

Anomalous harmonic lasing
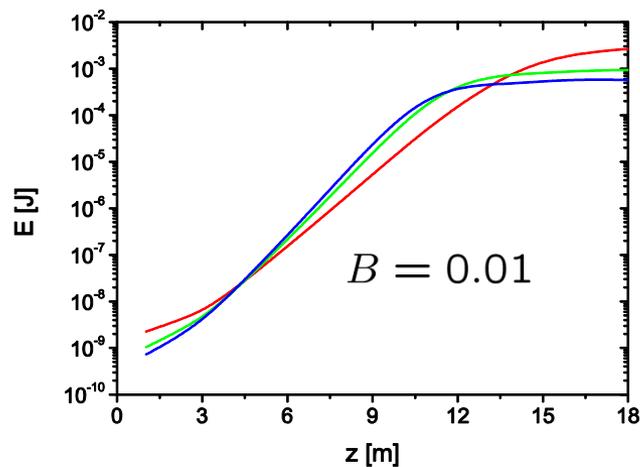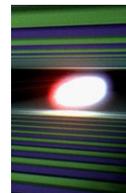
1st: red
3rd: green
5th: blue

$B = 0.01$

$B = 0.3$
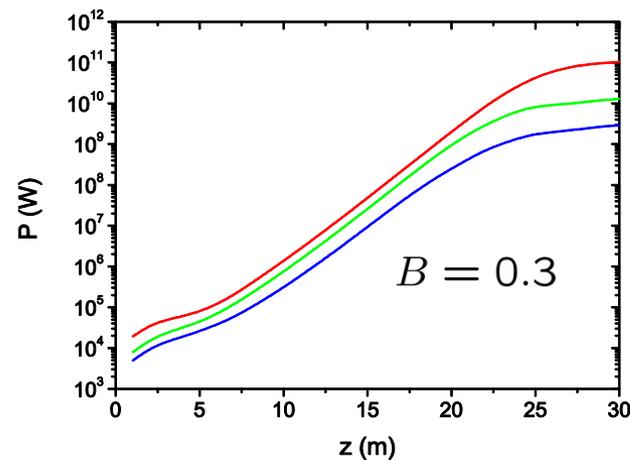
XFEL.EU: fundamental at 4.5 nm, beam energy 10.5 GeV, slice parameters for 100 pC from s2e, energy spread is 1 MeV

One can use this effect (in pump-probe experiments or for multi-user operation) or find ways to suppress it (if disturbs).
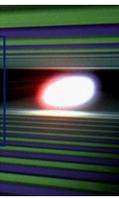
The case $2\pi\epsilon/\lambda \sim 1$ is typical for hard X-ray beamlines

If the same beam is used to drive a soft X-ray undulator (like SASE3 of XFEL.EU), the case $2\pi\epsilon/\lambda << 1$ is automatically achieved

For a reasonable beta-function one deals then with a small diffraction parameter $B = 4\pi\epsilon\beta\Gamma/\lambda$　　($L_g \propto 1/\Gamma$)

If the diffraction parameter is sufficiently small and K is sufficiently large, harmonics can grow faster than the fundamental!
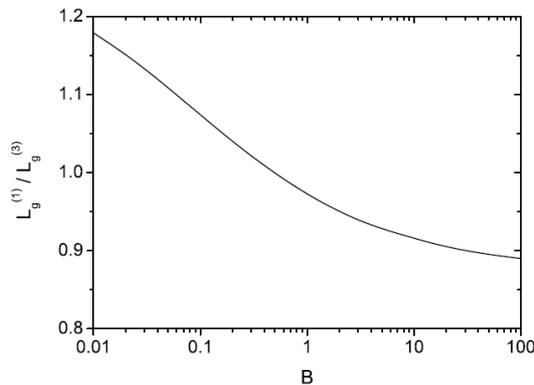
3D:　$\Gamma \propto (A_{JJ}^2\omega^2)^{1/2}$

1D:　$\Gamma_{1D} \propto (A_{JJ}^2\omega)^{1/3}$
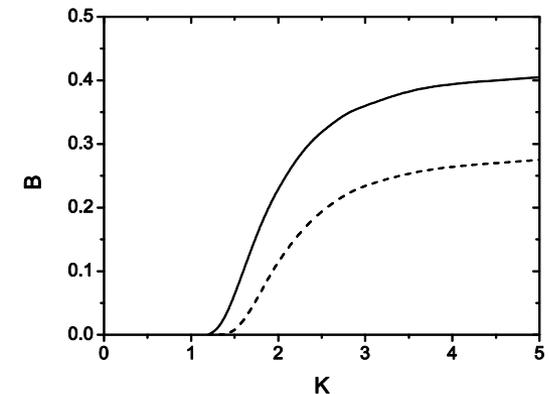
Fig. 4. Ratio of gain lengths for lasing at the fundamental wavelength and at the third harmonic versus diffraction parameter of the fundamental wavelength for large values of the undulator parameter K.
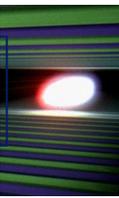
A. Harmonic lasing (with the suppressed fundamental) at some WL vs fundamental lasing at the same WL with reduced K.

$$\frac{L_g^{(1K)}}{L_g^{(h)}} = \frac{h^{1/2} K A_{JJh}(K)}{K_{re} A_{JJ1}(K_{re})}$$

$$K_{re}^2 = \frac{1 + K^2}{h} - 1$$

B. Harmonic lasing (with the suppressed fundamental) at some WL vs fundamental lasing at the same WL with increased beam energy.

$$\frac{L_g^{(1\gamma)}}{L_g^{(h)}} = \frac{h^{5/6} A_{JJh}(K)}{A_{JJ1}(K)}$$

Negligible energy spread, beta is optimized in all cases

Better than in 1D!
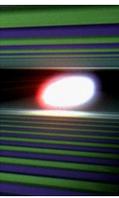
The method is proposed by McNeil et al., 2005
Parisi et al., 2005

If phase shifters are tuned such that the phase delay is $2\pi/3$ (or $4\pi/3$) for the fundamental, then its amplification is disrupted. At the same time the phase shift is equal to 2π for the third harmonic, i.e. it continues to get amplified without being affected by phase shifters.

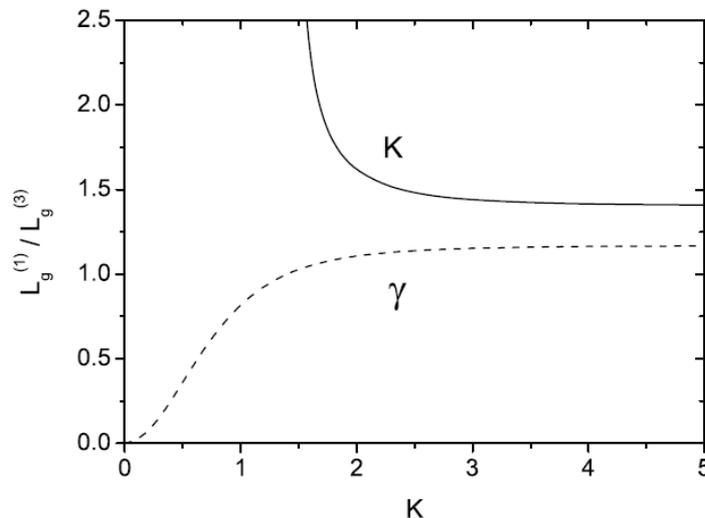Consecutive use of the same phase shifters, as proposed in McNeil et al., 2005 works well for a monochromatic seed but not for SASE. There is a frequency shift depending on number and magnitude of phase shifts.
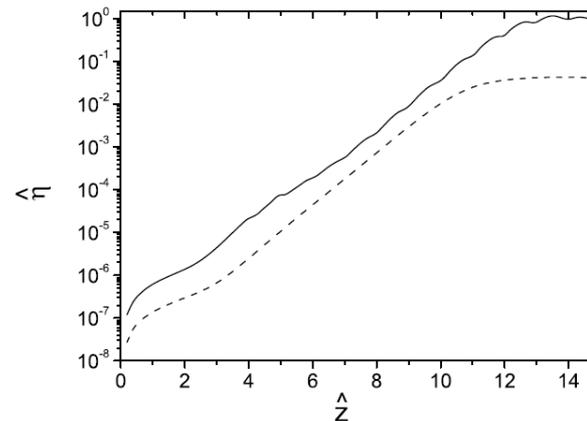
1D simulations

1st: solid
3rd: dash

A better method (alternation of phase shifts $2\pi/3$ and $4\pi/3$) is proposed in Parisi et al., 2005

Still not good enough!

Phase shifters (cont'd)
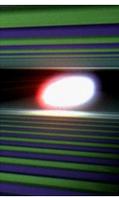
Piecewise use of phase shifters with the strength $2\pi/3$ and $4\pi/3$ suggested in Schneidmiller and Yurkov, PRST-AB 15(2012)080702, also NIMA 717(2013)37

1st: red
3rd: green

Proposal for FLASH upgrade, 1 keV;

49 phase shifters

Random distribution of phase shifters with the strength $2\pi/3$ and $4\pi/3$ suggested by Z. Huang, G. Marcus et al. (unpublished)

Conclusion: one needs a lot of phase shifters and a fancy distribution.

Energy spread effects
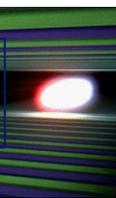
Harmonics are more sensitive to energy spread due to a higher mobility of particles (larger R56' in the undulator)

However, a reserve in gain length in the case of no energy spread lets harmonics be competitive with the fundamental also when the energy spread effects are significant.

XFEL.EU: Lasing at 1 A with 0.5 nC (current 5 kA, emittance 0.7 um)

Changing K

	1st	3rd
Energy	10.5 GeV	10.5 GeV
K_{rms}	1.05	2.3
Field L_g (no en. sp.)	10.4 m	6.9 m
Allowed en. sp.	2.8 MeV	

Changing energy

	1st	3rd
Energy	17.5 GeV	10.5 GeV
K_{rms}	2.2	2.3
Field L_g (no en. sp.)	7.9 m	6.9 m
Allowed en. sp.	1.3 MeV	
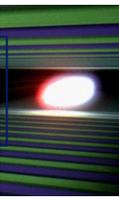
Higher harmonics are doing better for a large K and no energy spread

At some point there is a cutoff due to energy spread

There are technical issues (undulator field errors, undulator wakefields etc.)

The 5th harmonic lasing can still be considered practical in many cases

Lasing at 1 A with 0.5 nC (current 5 kA, emittance 0.7 um)

Changing K

	1st	5th
Energy	10.5 GeV	10.5 GeV
K_{rms}	1.05	3.1
Field L_g (no en. sp.)	10.4 m	5.8 m
Allowed en. sp.	2.3 MeV	
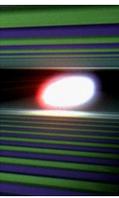
In the middle of the undulator the electron beam trajectory deviates from a straight line (chicane or closed bump), and a filter is inserted.
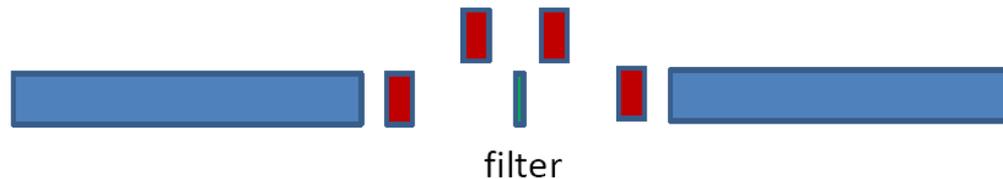
filter

Transmitted intensity scales as $\exp(-\mu d)$, where d is the thikness, and the coefficient μ depends on frequency as $a\exp(-b\omega)$. Very efficient high-pass filter due to the double exponential suppression.

Beam modulations are smeared through the chicane due to R56.

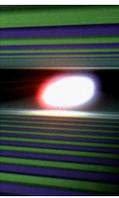Entrance of the second part of the undulator: no modulations, and only 3rd harmonic radiation.

Can be combined with a self-seeding setup: just add the filter!

If one filter is not sufficient: use two filters or a combination with phase shifters.
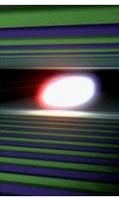
K is large enough, the 3rd and the 5th harmonics have about the same gain length:

3rd   5th

+ phase shifters

There can be more pieces:

+ phase shifters

R. Brinkmann, E. Schneidmiller, J. Sekutowicz, M. Yurkov, NIMA 768(2014)20

- Bandwidth: self-seeding   HLSS   SASE
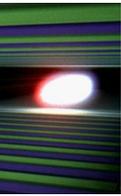- Power (previous slide):   HLSS   self-seeding   SASE (?)
- Intrinsic stability: SASE   HLSS   self-seeding
- Sensitivity to machine jitters: SASE   HLSS   self-seeding
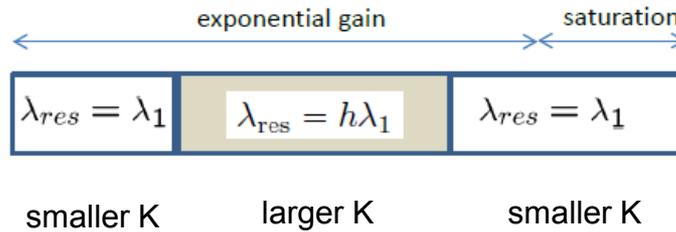- Setup time: SASE   HLSS   self-seeding

HLSS FEL promises a mild monochromatization, the highest power, a reasonable stability and robustness.

And …   HLSS is free!

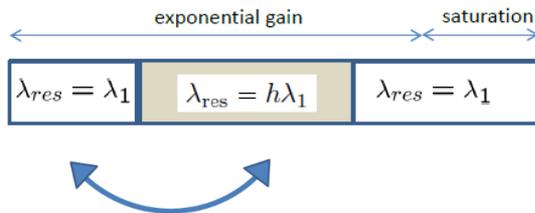A similar concept (pSASE): D. Xiang et al., PRST-AB 16(2013)010703

exponential gain   saturation

$\lambda_{res} = \lambda_1$	$\lambda_{res} = h\lambda_1$	$\lambda_{res} = \lambda_1$
smaller K	larger K	smaller K

First two sections are linear amplifiers (with large BW and small BW). One can swap them and keep the same properties of radiation in the end (small BW and high power):

pSASE FEL   HLSS FEL

exponential gain   saturation

$\lambda_{res} = \lambda_1$	$\lambda_{res} = h\lambda_1$	$\lambda_{res} = \lambda_1$

→

exponential gain   saturation

$\lambda_{res} = h\lambda_1$	$\lambda_{res} = \lambda_1$